

CAS PhD student statistics course

- **Lecture 1: Introductory comments and basic descriptive statistics**

- What is the point of statistics?
- Common pitfalls (confirmation bias, *a posteriori* statistics, systematic errors, low sample sizes)
- Calculating the mean, variance, median of a sample, and errors on those quantities
- Simple probability distributions: binomial, Poisson, Gaussian
- Error propagation (linear and non-linear)
- Optimal combination of data

- **Lecture 2: searching for correlations**

- Correlation coefficient and its error, regression lines
- How to quantify the significance of a correlation
- Bootstrap error estimates
- Non-parametric correlation tests (Spearman rank cross-correlation coefficient)
- Common mistakes: selection effects, outliers, cause & effect
- Comparing two distributions (K-S test, comparison of means or variances)

- **Lecture 3: hypothesis testing and model-fitting**

- Hypothesis testing and goodness-of-fit: χ^2 statistic and distribution, degrees of freedom, p -value, reduced χ^2 , inclusion of correlated errors, common mistakes in interpretation
- Parameter estimation, relation between χ^2 and likelihood
- Quoting 68% and 95% confidence limits, how to describe skewed distributions and asymmetric errors, correlations between parameters
- Is adding another parameter justified by the data?
- Marginalization of parameters

- **Lecture 4: Bayesian inference**

- What is meant by “Bayesian” and “Frequentist” statistics?
- Bayesian inference, conditional probabilities, importance of priors, model selection, information criteria
- Monte Carlo methods